# FLUID MECHANICS



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## 5.6 Orcifice, notches and weiry

5.1 Define orifices.

5.2 flow through orcifice

5.3 Orifice coefficient and the relation between the orifice wefficients.

5.4 clanification of notches and weirs.

5.5. Divehange over a rectangular notch on wein

5.6 Dinharge over a trianguleur notch on wein.

5.7 simple problems on above.

## 6.0 pro Flow through pipe

G. Definition of pipe

6.2 Low of energy in pipe

6.3 Head low due to frietion: - Dancey's and

chery's foremules 6.4 volue problem using Darcey's and cherujs tornelle.

6.5 Hydraulic gradient and gradient line.

## 7.0 Impact of jet !-

7:1: - impact of jet on finee and moving ventical flat plates.

7.2: - Dercivation of workdone on ser vanier and condition for maximum efficiency

7.3: - impact of jet on moving curved varies illustreation wing nelbrity atricingly derivation of workdone, efficiency. coally the to war !

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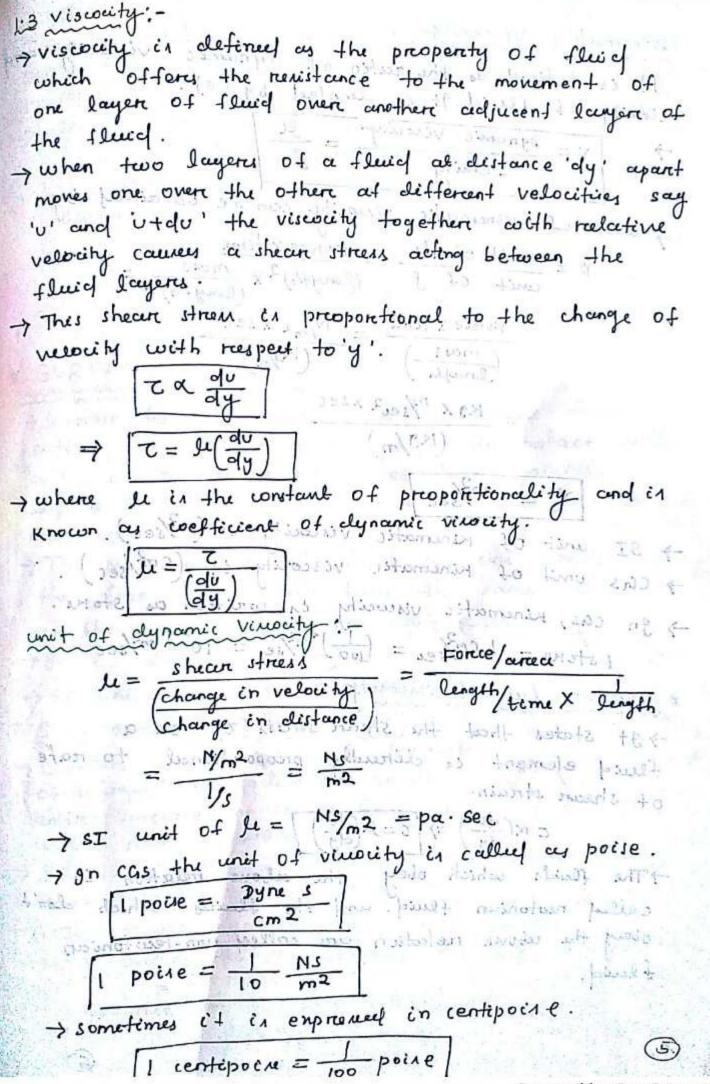
Door from themselve | business of the same

of solve single praisers.

Later to trained

PROPERTIES OF FLUID :-1.1-: Define Fluid: -> Fluid may be defined as a substance which is capable of flowing. It has no defenite shape of its own, but it takes the shape of the containing vessel. -> Further even a small amount of shear force crenteel on a fluid will course it to undergo a deforemention which continues as long as the forece continues to be applied. The fluides are also colonificed as colered fluid and road fluid. Ideal fluids are those fluids which have no viscocity and surface tention and they are incompressible. Ideal fleids are only imaginary fleids. -> Real fluids are those fluids which are actually available in nature. There fluids pouru the properties week as viscouity, unface tension a compressibility. stable in toge 1.2 properties: pently to himse 79+ is defined as the reater of mass and volume. (a) Denuity (3) :-7 St is denoted by symbol (3) -> SI unit of density is (Kg/m3). As as & = 1m/v | was only men and with + denity of water (3) w = 1000 kg/m3. -> denity of air Sain = 1.208 kg/m3 .... -> denity of seawater (8)s.w = 1025 kg/m3... of (b) specific weight: → 94 is defined by weight per unit valume. 79+ it denoted by symbol 'wi 7 SI unit of specific weight in (N/m3) co = weight is plant = whiten = sting (iii)  $cw = \frac{mq}{V} = \left(\frac{m}{V}\right) \times g = f \times g$ 

-> specific weight of water = 1000×9.81=9810 N/m3 -> 'w' depends upon g and denity . so 1+1 value also depends upon temperature and pressure. LC) Specific volume :-> specific volume is generally defined as the volume of the fluid per unit mass ... + It is reciprocal of clemity. + In SI unit the specific weight is expressed in (m3/19) -> 9+ in denoted by 'v'. marter and and allered (4) Specific Granity: -> specific granity is defined as the rectio of density of fluid to the density of standard fluid. -> For liquids, standard fleid in taken as water and fore gases the standard fluid in taken of air. -> 9+ or denoted by 's'. S = Denity of fluid Denity of standard fluid -> The value of specific granity of water = 1 \* Problem-1 calculate the specific weight, clenity and specific gravity of 1 et of a leigned which weights 7N. Data given! volume = 1 litre = (1000) m3 weight = 7 N. (1) Specific weight (co) = weight volume (ii) Denvity (3) = specific weight = 7000 = 713.5 kg/m3 (iii) specific growity = dmity of liqued durity of water 713.5 =0.7135 1000



-> Kinemate c viscocity It is defined as the reation of dynamic vinescity and doning of fluid. It is denoted by (v). V = Dynamic Virolity - unit of minematic vinocity can be obtained by Dz unit of le = Force x time (lungth) 2 x (longth) 3 Force x time = N/m2 x sec 111 = Kg x M/sec2 x sec (K3/m) To = m2/sec Instruct with SI unit of Kinematic viscocity ca (m3/sec). > cas unit of Kinematic viscocity is (cm/sec) -> In cas, kinematic visucity is written as stoke. 1 stoke = 1 cm/ser = (100) m2/ser = 10-4 m2/sec. \* Newton's Law of Viscouty > It states that the shear struss (2) on a fluid element in directly proportional to rafe of shear strain.  $\tau \propto \left(\frac{dv}{dy}\right) \Rightarrow \tau = \mu\left(\frac{dv}{dy}\right)$ The seweds which obey the above relation is called newtonian fluid, and the fluids which don't obey the above relation are called non-recutorian fluid. expressed to control of Lorent towns

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problem Two horizontal plates are mept 1.2 cm apart. The space between them being filled with oil of viscocity 14 poine. collectate the shear stress in oil if upper place on moving with a velocity 0-f 2.5 m/sec. dy = 1.25 cm = 0.0125m. le = 14 poise = (14) NS/m2 shoeir stress z= H(du)  $\Rightarrow$   $\tau = \frac{14}{10} \times \frac{2.5 - 0}{0.0125}$ Z = 280 N/m2 \* SURFACE TENSION . -> Sureface tension is defined as the tensile force acting on the uneface of a liquid in contact with a gas ore on the surface between two immissible liqueds such that the contact unface behaves like a membrane under tenion. The magnitude of the force per unit length of the free rureface will have the name value as the uniface energy per unit area. ->9+ in denoted by (0-). > SI unit of unface terrion (N/m) \* Surface ternion on liquid droplet. oniclere a small spherical drepplet of a liquid of readily it', on the entitle rereface the tenule forcce is acting due to unface tencion. > 9f the droplet is cut into two halms the force acting on one half will (i) The tensile force due to surface tension acting acround the circumferance Of the cut portion => force on the arrew = PX Tyd2 Lund 1900 1 =>PX Tyd2 = TXTI

\* Surface tennion on soap bubble: -A hollow bubble like a soup bubble in air hay two surfaces in contact with aire one imide and

one outside.

-> Thus two surfaces are subjected to runface tension => Px 1/42 = 2x0x 119

\* Sureface tennion on liquid jet!

$$\Rightarrow P \times A = \sigma \times (21)$$

$$\Rightarrow P \times 1 \times d = \sigma \times 21$$

$$\Rightarrow P = \frac{2\sigma}{d}$$



Find the unface tenion in a roap bubble of young diameter when the invide prevene in 2.5 N/m2 above atmospheric pressure.

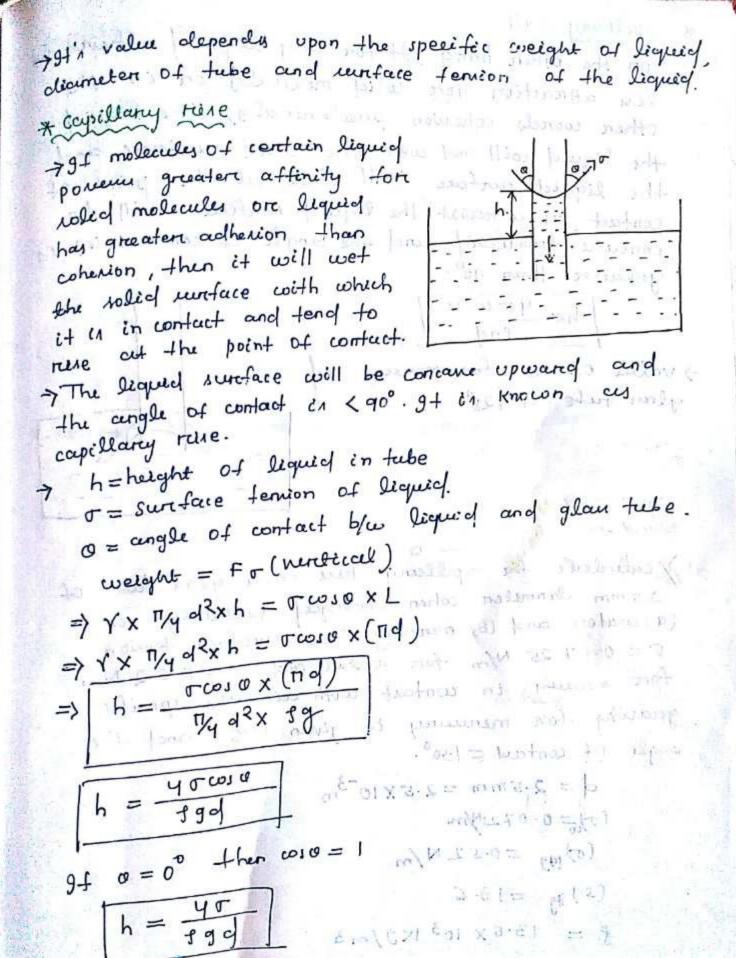
Civen 
$$\beta = 40 \text{mm} = 40 \times 10^{-3} \text{ m}$$
 $P = 2.5 \text{ N/m}2$ 
 $\Rightarrow P = \frac{80}{9}$ 
 $\Rightarrow 2.5 = \frac{80}{40 \times 10^{-3}}$ 
 $\Rightarrow 80 = 0.0125 \text{ N/m}$ 

LARITY:

CAPILLARITY: - - June James James June 10 miles + capillarity is defined as a phenomenon of reise on fall of a liquid when the tube is held ventecally in the liquid.

7 The rive of liquid writage is known as capillary rise whereas the fall of liquid surface is known as capillary fall.

> 91 is enpressed in Com of liquid. PHKE - S NO XAGE



on the other hand, It for any lequid theire on the other hand, I for any lequid on in the len attraction for rolid molecules on in the lequid will not wet the rolid runfaces and the liquid runfaces will fall at the point of confact, as a rosul the liquid runfaces will be concause downward and the angle of confact (6) of greeder than 90°.

h= 45 cosca pad plan tube 11 128°

Compared the capillary there in a glaw tube of 2.5 mm diameter when immerged vertically in (a) water and (b) mercury. Take runtface tension T = 0.07.25 N/m for water and T = 0.52 N/m for mercury in contact with air The specific

sdu'ni buy 5=12-44-1

gravity for mercury is given 13.6 and the angle of contact = 130°.

 $d = 2.5 \text{mm} = 2.5 \times 10^{-3} \text{m}$   $(\sigma) = 0.0721 \text{N/m}$   $(\sigma) = 0.5 2 \text{N/m}$  $(s) = 13.6 \times 10^3 \times 9/\text{m}^3$ 

capillary rise for water
$$h = \frac{4r}{19d} = \frac{4 \times 0.0725}{1000 \times 9.81 \times 2.5 \times 10^{-3}}$$

$$= 0.0118 \text{ m} = 1.18 \text{ cm}.$$

$$\text{capillary rise for mercy}$$

$$h = \frac{4 \text{ cos 0}}{190}$$

capillary rive for metaly
$$h = \frac{40 \cos \alpha}{400}$$

$$0 = 130^{\circ}$$

$$h = \frac{4 \times 0.5.5 \times 0000 \times 9.81 \times 2.5.}{13.6 \times 10000 \times 9.81 \times 2.5.} \times 10^{-3}$$

\*. negative vigo indicales the capillary deprenion.

CHAPTER-2 2.0: - FLUID PRESSURE AND ITS MEASUREMENT! pressure intensity. preserve intensity may be defined as the force enercted on a unit area. If 'F' represents total force unistormly distributed over an area 'A', the presure at any point P=(F/A). It the force is not uniforumly distributed, the expression will give the average value only sections -) when the presume varies from point to point on an arrea, the magnitude of prevene at any point can be obtained is action presume horse unit:-SI unit of presume N/m2 ore posscal 1 Kpa = 1000 pa = 103 N/m2 1 ban = 105 pa = 102 kpa = 100 kpa = 10 N/m2. presume variation in a fluid at rest: --> The presence at any point roin a fluid at rest in obtained by the hydrostatic rate of increase of presuntant sinely into in a vertically downward direction must be expal to the specific weight of the fluid at that point to me of no reduce to > DA = cross rectional arrea of the element. OH = height of the fluid element. p = precione on face AB Z = distance of their element from free unface. -> premere force on AB = PX AA

CD = (P + ( P) DZ ) X DA

12)

-> weight of I lied = JX ) X (DAX DZ) preum force on AB and CD are equal and opposition  $\frac{\partial f}{\partial z} = f \times g = \omega$ 1 porus low & no la a for = figor and men lested and the

7 where p is the presume above almosphere a presum an Z is the height of the point from free aerface.

> z is called premure head

#### 22 pascul's Law ! -

SEL.

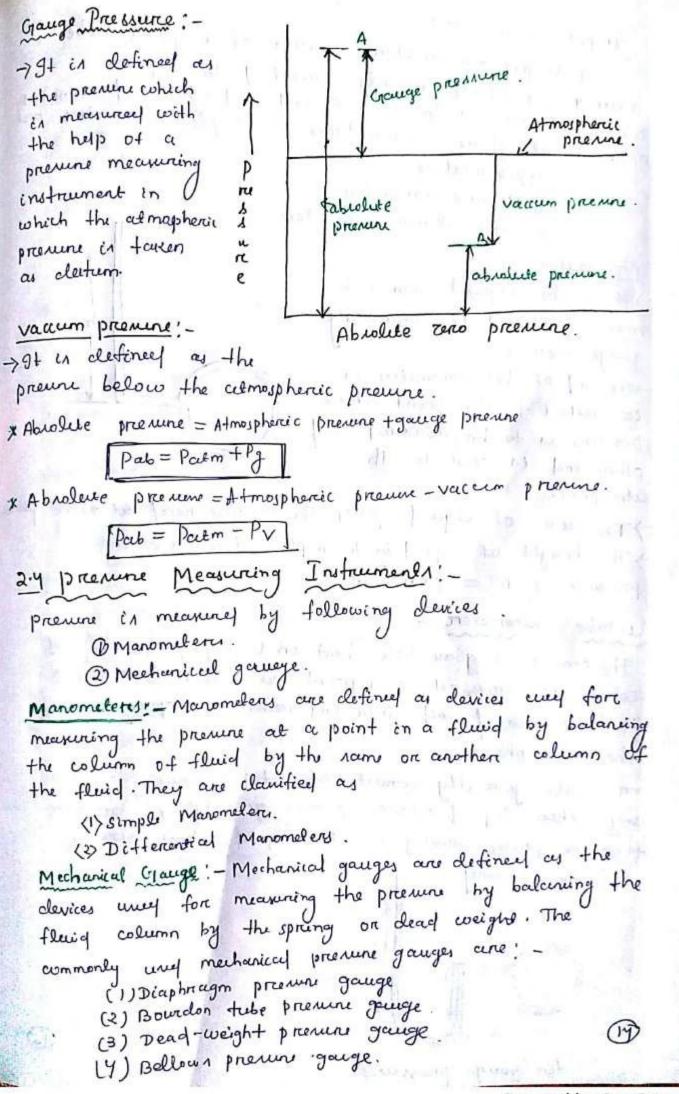
9+ stades theet the presume on intensity of presume at a point in a static fluid is equal in all direction. Px = Py = Pz | 301 = 100 1 = 100 1

-> prevene at any point in x, y, z directions in equal. trication and point 2.3 Atmospheric premine:

The almospheric aire energy a normal presume upon all runfaces with which it is in contact. It is Known ou ofmarpheraic premine.

- -> The atmospheric presure varies with altitude and it can be measured by using barrometer.
- > value of atmospheric presune = 101.325 14pq. on 10.3 m of water on 70 cm. Of mercury Abrolute premie :-

The presume mecured with reference to absolute vacuum/zero (complete vaccum) then that is called as aboroletie premere. 20 = ( P ) ( 1 th ) D = 03



A simple amanometer cominer of a glan tube Simple Manometers: having one of ithis ends connected to a point where pressure is to be measured and other end remains open to almosphere . common types of simple manometers O piercometer 3 80 - tube manometer 3 single column manometers. Die cometer : -->9+ in the simplest form of manometer used for measuring gouge presure.

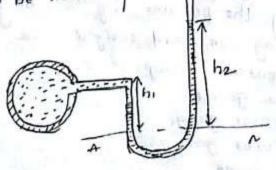
-> one end of their manometer in connected to the point where presure is to be measured and other end in open to the

> The rine of liquid gives the premure head out that point > The height of liquid is 'h'in pierometer tube the presume at 'A' = 89xh N/m2

U-tube Manometera! -

> 9+ cominds of glass tube bent in U-shape, one end of cohich is commuted to a point out which presume is to be measured and other end remains open to the atmosphere.

The tube generally consists of contains merceuny ore any other liquid whose specific granity is greater than the specific granity of the liquid where presume is to be measured.



fore gauge pressure.

for gauge presure:-

B in the point out which produce in to be measured, whom value is &p. The clatum line is A-A. h = Height of liquid above dutum line. h\_ = height Of heavy It quid above datum line. S, = specific granity of light liquid Sz = specific granity of heavy liquid Of = Denity of light liquid = 1000xs,

82 = density of heavy liquid = 1000x52

As the premure is the same for horizontal unface, The precure above the horizontal datum line in the left column, and in the reight column Of U-tube manometer should be same.

presure above A-A in the left column = P+3, gh, presume abone A-A in the right calcum = 829 hz. Hence equating the two premere

for vacam promise:for measuring vacuum premery the level of the herry lique of in the manometer will be

presure above A-A on the

left column = p+ 329 hz+8,9h, A present hered in the reight column above A-A = 0.

$$g_2gh_2+g_1gh_1+P=0$$
  
=>\P = - (\frac{g\_2gh\_2+g\_1gh\_1}{g\_2gh\_2})

(3) Simple v-tube manometer containing mercury in connected to a pile in which fluid of sp. greanity of and having vacuum previews in flowing. The other end of the manometer in open to atmosphere Find the vacuum presume in the difference of mercury level in the two limbs in your and the height of fluid in the fell trom the centre of pipe is 15 cm. below.

Ans Specific greatity of liquid 51=0.8.

sp. gravity of Hg = 13:6.

g. of liquid (f1) = c1×1000

= 0.8×1000

= 800.

g of merceny (fz) = 13.6×1000 = 13600.

hi= 15cm = 0.15m.

h2 = youm = 0.4m.

p+ f2gh2+ f1gh1= 0.

> p = - (119hi+ 129 h2)

-- (800× 9.81×0.12) +(13600× 9.81× 0.4)

the bearing to and

= - 54 54 3 · 6 N/m2 = -5 · 4 5 N/cm2 (Ans)

mencuray is connected to a pipe in which current of spi

(a) 2. The reight limb of a simple u-tube manometer containing marauny is open to the atmosphere cohile the left limb is connected to a pipe in which a fluid of sp. gravity is org is flowing. The centre of the pipe is larm below the level of mercury in the right limb. Find the pressure of fluid in the pipe if the obtferences of mercury in the two limbs is 20 cm.

SINGLE COLUMN MANOMETER: -

gingle column manometer is a modifieef form a u-tube manometer in which a reservoir, having a large cross sectional area as comparred to the area of the tube in connected to one of the limbs of the manometer. There are two types of single column manometer as :-

O Veretical Single column Manomelen

@inclined single whem manometer.

= 32 ×9 ( 1+h2).

Overfical single column manometer:~

> 9+ shows the neithicrate aringle; column manometer. -> x-x be the datum line 10th of blues in the reget limb of the manager is the right limb of the manager is the region of the region o - when the manometer : (12.5) connected to the pipe. at A', the heavy liquid due to high promene on the renember will be pushed downward and will rune in the reight limb. -> sh = fall of heavy liquid in remeroion. hr= rince of hemy liquid in right limb. PA = presure out A which to be measureef. A = cron rection of the remervoien a = coron rectional area of reight limb S., zspecific growity of liquid in pipe. Sz = 5 p. granity of heavy liquid in renembien In = density of liquid in pipe Be = denity of liquid in neveruoien. Axh = axh 2 = Dh = (a) x h2 premune in the reight limb about Xxx Xxx Y- Y

presure in the left limb above Y-Y= SIX9X(Dhthi) +PA. equating them previous 82xg x (0h+h2) = 31xg x (0h+h1)+PA => PA = \$2x9 (Ah+h2) - \$1x9 x (Ah+h1) = 1h (129-119) + h2(29-h1919.  $\Delta h = \frac{q_x h_z}{\Delta}$ a) A single column manometer in connected to a pipe confuering a liquid of 17. greenity as whom in fig. Find the presure in the pipe of the neverwien in 100 times the area of the tube for the monometer receling. The specific gravity of menery in 13.6 9,=0.9 11 = 90 0 Kg/m3 £ = 13600 " b. \$ = 100. hi = 20cm = 0.2m h2 = 40cm = 0.4 m PA = = = h2[ f29-8,9]+ h2 529 - h1 519 = 5.21 N/cm2.

## DIFFERENTIAL MANOMETERS

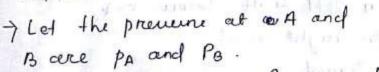
differential manometers are the clevices were fore measuring the difference of previous between two points in a pipe on in two different pipes. A differential manometer commits of a U-tube, confaining a heavy liquid, whom two ends are connected to the points whom difference of pressure is to be measured.

(2) Invertee U-tube differential manometer.

1110-tube differential Manometers: -

The two points A and B are at different level and also contains liquids at different Sp. granity. X

There points are connected to the U-tube olifferential manonuser.



-> h = difference of Hy level in the U-tabe.

- Y = difference of centre of B from Hy level in reight limb.

X = difference of centre of A from Hy level in centre

of liquid at A

B2 = 1/2

equating the two premies Sig(h+n) + PA = fg x. g x h + f2x g x y +PB => PA-PB = fgx gxh + f2xgxy - f1xg (h+r) = hxg (3g - 31) + 32xg xy - 31xg xx Invertee U-tube differential manometer. -> 9+ commits of an inventer u-tube containing a light liquid, 97 is weel for measuring difference of low premuu. -> The two ends of the tube are connected det two points whose difference in premine is to be measured. > Let the promine on 4 is ( more Than B. he=height of liquid in left limb below x-x hz = height of liquid in reight limb. h = difference in light liquid 31 = de Denvity of liquid at 'A' Iz = Deruity of liquid at 'B'. By = denity of light liquid. PA = presure cet 'A' in frame to the men PB = precene cut 'B'. premere in the left limb above X-X = PA-fig Xh, present in the right limb below x-x = PB - Jzg /2 - 5gJh. equiting A ( day the PA - 8,9 h1 = PB - 82 Jhz - 899 h => PA-PB = \$17h1-J27h2-99h

of Addisservential manomiler continued by the two points A and B of two pipes and whoman Therepend. contains a liquid of specific greatify = 1.5 while pipe B contains or liquid of sp. granity = 0.9. The priority act and B are 1 K9f/cm2 and 1.80 kg f/cm2 respectively. find the difference in mureuy level in differentical moinomet en PA = 1 kg f/cm2 = 1 x 1 0 / kg f/m2 = 10/x 9.81 N/m2 PB = 1.8 Kg-/cm2 =1.8 x 9.81 x 10 1 N/m2 left limb 1. = 13.6×1000× 9.81×h + 1500×9.81× h. tone bises to and to report courses the fleric two pipes A cence to volvery or go of some A spile out to single of the property of the state of the property pressure elifterence blu A and B. , A pipe contains an oil of sp. gravity of 0.9. A differential manometers connected at the two points. A and B shows a difference in mercuny Junel cy 15-cm. find the difference of presume at two points. S1 = 0.9 3, = 0, 9x1000 h = 15cm. sg = 13.6.

if A differential manometer is connected at the two points A and B ou who con in figure. At air presume in 9.81 N/cm2. Find the absolute premine at 'A'. 8, =0.9×1000 = 900 Kg/m3 presure in the left limb = Garre PA + 900 × 9.81 × (20) + 13600×7.81×10 present in the right limb = PB+ 10000 1000 X 9. 81 X 60 equesting PA + 900 x 9.81 x 0.2 + 13600 x 9.81 x 0.1 = PB + 9.81 x 1000 x 0.1 => (PAT Pro) = PA = 8.887N/cm2 a) An invented differential manameters is connected to two piper A and to which convey worken. The fluid in manometer is oil of sp. growing 0.8. find the present difference b/w A and B. 51=0.8. 8, = 800 Kg/m3. in the left limb = PA -1000 x 9. 81 x/30 in right limb= PB-1000 x 9-81 x 0.3-800 x 9-81x 0.2 => PA-2943 = PB-4512.6 => |PB-PA = 1569.6N/m2 20cm.

Boundon Tube Pressure Crange:

> 91 th the most common type of premere gauge which was invented by E-Boundon.

-> The presume responsine element in this gauge is a tube of steel on bronze which is of diptical cross-section and owney into a cinculture arc.

- The tube is closed at its outer end,

and this end is free to move.

-> The others and of the tube + through which the fluid entens in reigidly times to the frame, when the gauge is connected to the gauge point, fluid under pressure enteres the tube.

-> Due to increase in interenal pressure, the elliptical crownection of the tube tonds to become circulain. thus causing the tube to straighter out slightly.

of the small outward movement of the free end of the tube is transmitted, through a link, quadrant and pinion; to a pointer.

> The pointers moves clockwise on the greateched circular dial indicales the pressure intenity of the fluid.

> The deal of the gauge in so caliberated that it reads zero when the pressure imide the tube equals to the local almospheric pressure.

# HYDROSTATICS (CHAPTER-3)

Jotal Prossure: -

Total pressure is defined en the force exercised by a static fluid on a runface wither plane or current when the fluid comes in confact with the runfaces.

This force always and normal to the runface.

centre of pressure: 
centre of pressure is defined on the point of application

of the total pressure on the surface.

vertical plane surface submerged in liquid:

comider a plane ventical unface ubmeraged in a liquid.

A = total area of the unface

To = distance of c.G of the circu from free surface of liquid.

G = centre of granity of plane unface

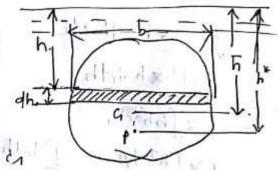
p=centre of preserve.

hx = centre of presune from free unface of liquid.

The total pressure:

The total pressure on the sunface may be determined by dividing the entire surfaces into a number of pullable strips.

The fonce on small strup



then concered and the total presum force on the whole area is calculated by integrating the force.

> Consider a streep of thickness of h and width b at a depth of h from free surface of liquid.

prenume intenity aton the strip = soft

Area of the strip = dA = bxdh

total force on the strip dF = pxarec
= sghxbxdh.

F = SolF = Soghxbxdh

> Sox bholh

= hosy Shith

= sox masshxda

# F = 39XAX F T POTGAPY STITATEORY

A = Area of unface To = distance of .C. G from the free reverage

-> centre of preseure is calculated by wing principle

-> preinciple of momenty state that the moment of the remutant force about an aris is equal to the sum of the moments of the components about the same anis. -> The resultance force F is acting at Pat a distance

It from free renface of the liquid. -> ryoment of the fonce 'F' about free uniform = FX 1/2

-> Moment of force dF, creating on a strip cobout free

junface = d FXh.

= jghxbxdhxh.

Sum of forces of all such forces about free surfage

$$= \int f g h \times b \times dh \times h.$$

$$= f g \int b \times h \times h dh$$

$$= f g \times \int b h^{2} dh$$

$$= f g \times \int h^{2} dh$$

TOX AXT AR

from parallel anis theorem we have

[Io = Ia + Ax Ti2]

In = Moment of inertia of area about an anis

powing through the C.4 of the area and parallel

10 the free unifour of the liquid.

 $h^{*} = \frac{I_{G} + A \times h^{2}}{A h} = \frac{I_{G} + A \times h^{2}}{A h}$ 

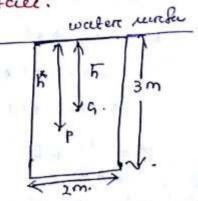
plane unfal   the ball	Aree	Ig	<u> </u>
1. Rectargle n = d/2	Ь	693/12	b43/3
2. Treiangle $x = h/3$	bh/2	bh3/36	b 43/12
3. circle  3. circle  1 = 01/2	ग्मव्हें पू	π « <sup>1</sup> / <sub>6</sub> γ	X

Of A rectangular plane unface in 2m wide and 3m deep. It lies in vertical plane in water. Deformine the total presure and position of centre of presure on the plane surface when its upper edge is horizontal and coincides with water unface.

(b) 2.5 m below he free water leerface.

 $F = 3g \times A \times \overline{h}$   $f = 1000 \times g/m^3$   $g = 9.8 \, m/g^2$   $A = 3 \times 2 = 6 \, m^2$   $A = 3 \times 2 = 6 \, m^2$   $A = 3 \times 2 = 6 \, m^2$   $A = 3 \times 2 = 6 \, m^2$   $A = 3 \times 2 = 6 \, m^2$   $A = 3 \times 2 = 6 \, m^2$ 

F = 1000 X 9.81 X G X 1 .5 = 88290 N.



$$I_{4} = \frac{I_{5}}{Ah} + h$$

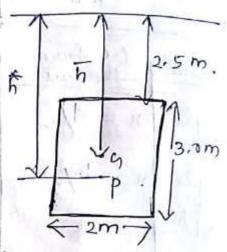
$$I_{4} = \frac{bh^{3}}{12} = \frac{2\times3^{3}}{12} = 4.5m^{4}.$$

$$I_{5} = \frac{4.5}{6\times1.5} + 1.5^{-} = 2.0m.$$
(b) upper edge in 2.5m, below water unifore.

F = 89 x A x h

$$F = 2.5 + 3/2 = 4 m$$
,

 $F = 1000 \times 9.81 \times 6 \times 9$ 
 $= 23.5440 N$ 
 $F = \frac{I_9}{AF} + F$ 
 $= \frac{4.5}{6 \times 9} + 9 = 4.1875 m$ .



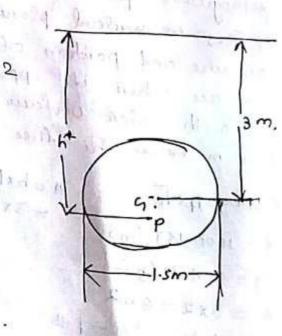
of Deference the total presence on a circular plate of diameter 1.5 m which is placed vertically in water in much a way that the centre of plate is 3m below the free reinferer of coulen find the position of centre of preseure.

the of precione.

$$d = 1.5m$$
 $A = \frac{\pi}{4} \times (1.5)^2 = 1.767m^2$ 
 $h = 3m$ .

 $F = 3x9x4xh$ 
 $= 1000 \times 9.81 \times 1.767 \times 3$ 
 $= 52002.8 N$ .

 $h = \frac{\pi}{4h} + h$ 
 $\pi = 3.0468 m$ .



\* Horizontal plane lunface

> Consider a plane horizontal

> funture immerged in a static fluid.

> An 'G' and 'P' cure at the name

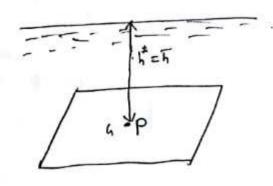
- depth from the free uniface of

the liquid, the presume intensity

A = total area

= Sghx A

F = SgAX To



3.4 Archimedes principle:

>9+ states that when a body is immercycel in a fluid either wholly or partially, it is littled up by a fonce which is equal to the weight of the fluid displaced by the body. - Acoording to Archimedes principle it in therefore known that the broyant force is aqual to the weight of the fluid displaced by the body.

BUOYANCY :-

when body is immerged in a fluid either wholly on pointially it is subjected to an upward force which fends to lift it up. This tendency fore an immerged body to be lifted up in the thuid oleve to an upwared force opposite to the action of granity is known as brogary. -> The fonce tending to lift up the body under such conditions is known as buoyant force.

centra of bevoyancy:

9+ is defined as the point through which the force of buoyancy is responsed to cut.

-> The centre of buoyances will be the centre of greenity of the fluid displaced,

Meta centre Norumal displacement

-79+ in defined as the point about which a body starts Ostillating when the body in titled by a small angle. The meta centres may also be cletined as the point at which the line of action of the fonce of buoyany will meet the rounal amis of the body when the body in given a small anguleur displacement.

-) consider a body floating in a liquid our shown in figure. Let the body is in equilibrium and is the centre of granity and B the centre of buoyaney. -> fore equilibrium, both the points lie on the normal cinis, which is verdical. per plante medice pault r of laspusones stant \* The distance between the centre of granity of flociting body and the metacentre (GM) is called metacentric height.

Types of equilibrium of floating bodies: the equilibraium of floating bodies in of following types Ostable equilibrium Dunstable equilibrium 3 Newtral equilibrium.

## Kinematics Of flow

-> Kinemation in defined as the breament of suience which deals with motion of particles without considering the forces causing the motion. The shuid motion is described by two methods.

B Lagrangian method.

@ Gulerian method.

of the lagrangian method a single fluid particle is followed during its motion and its relocity, acceleration, denity are descent beef.

> 90 Eulerian method the velocity, acceleration, precure, denity are described at a point. The fullerium method

is commonly used in fluid mechanics.

Types of Flow :-

O steady and uniteally Slow

Quaiform and non-uniform flow.

3 Laminar and turbulent flow

@ Compressible and incompressible flow

Grafational and innotational flow

@ one, two and three dimensional flow.

Osteady and unsteady flow!

-> steady flow is defined as that type of flow in which the sluid characteristics like velocity, presure, density at a point don't change with time.

I for steady flow  $\frac{\partial V}{\partial t} = 0$   $\frac{\partial P}{\partial t} = 0$ ,  $\frac{\partial Y}{\partial t} = 0$ . tursteady flow is defined as that type of flow in

which the velocity, premure and demity are a point Changes with respect to time

@uniform and nonuniform flow: uniforem flow is defined as that type of thou in which the nelocity at any given time does not change with respect to spacee Clength of direction of the for uni-form flow  $\left(\frac{\partial V}{\partial S}\right)_{t=c} = 0.$ av = change of nelocity 25 = Length of flow in the direction -> Non unioform flow is that type of flow in which the nelocity at any given time changes with nespect to specele for non uniform flow (a) )t=c + of 3 compressible and incompressible flow! -> compressible flow a that type of flow in which denity of slewid changes so from point to point , the demity (s) is not constant fore the fleriof. -> Incompressible flow is that type of flow in which the denity is contact for the fluid flow. for imamprecially Slow [3=0]

(4) Laminan and tunbulent flow: -> Laminare flow or defined as that type of flow in which the fluid particles more along the stream I This tupe of some and stream lines are straight and parallel. -> This type of flow are also called on streamline flow. -> for magnotet no claminar schow payned of No = VD (21" of the particles move rig ray way, or which the fore turbulent flow [Ra > 4000]

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potational and irrotational flow:

potational flow is that type of flow in which

the sheid particles while flowing along the streamline

also rotate about their own anis:

Travotational flow is defined as their type of flow in

which the fluid particles flowing along the stream

line do not rotate cebout their own anis.

Gone-dimensional, two-dimensional, three-D flow:

pore-dimensional flow is that type of flow in which the

flow parameter such as relocity is a function of tome

and one space wondincte only.

and one space coordinate only.

The variation of velocity in other two mutually to direction is assumed to be regaligible.

> U=f(x), V=0, and W=0.

Two dimensional flow is that type of flow in which the flow parameter such as velocity is a function of time and two space coordinates such as a and y.

The variation of velocity in and direction is negligible.

U=f(1,4), V=f2(1,4), W=0

> 3 dimensional flow is that type of flow in which the velocity is a function of time and 3 mutually spare correlinates.

U=fi(n,4) V=fz(n,4) \* W=f3(n,4,2).

Rate of flow on Discharge

9+ in defined as the quantity of a fluid thowing per record through a recetion of a pipe.

 $(m^3/_3)$ 

A = cross sectional area of pipe v = average nelocity of fluid.

Continuity Equation

The equation boused on the preinciple of comerwation of mass is called continuity equation.

- Thus for a sluid flowing through the pipe at all cross-section, the quantity of fluid pended commidere 2 constant

-> comuder 2 sections @ and 2)

-> VI = average velocity at cross nection 1-1

P, = density at section 1-1

AI = Arece of pipe at 1-1

V2 = owenage velocity cut kross section 2-2

f2 = demity out section 2-2

A2 = Area of pipe cel 12-2

The note of flow at rection -1-1= BIAIVI

The nate of flow at rection 2-2 = f2A2V2

According to law of convertation of mass

nate of flow at sertion 1-1 = nexte of flow at 8, A, V1 = \$2A2V2 | Section :-1

-> It is known as continuity equation. if the fluid is incompressible

 $f_1 = f_2$   $A_1 \vee_1 = A_2 \vee_2$ 

The diameters of a pipe cut the 1-cetion 1 and = 201 form and 15 cm reespectively. Final the discharage through the pipe if the relouity of wellere I lowing through The pipe at section of in smill. Thenof nelocity at ment a = +1 1 = 0. 0 8 7 2 7 mb/a.

AIVI = AZVZ

=) V2 = 2.22 m/s.

of A 30cm pipe containing conter, breamher into two pipes of diameters soom and isom respectively. If the ang. relocity in the 30 cm pipe in 2.5m/s find the climberrage in the pipe. Also oldermine the nelocity in 15 cm pipe if the owg. nelocity in som pite in 2m/s. D1=30cm=0.3m AI = T4 D12 = 0.07068 m2 V1 = 2.5 m/s V1 = 2.5m/s. D2 = 20 cm = 0.2 m. A2 = Tyx(0,2)2 = 0.0314 m2 V2 = 2 m/s 21 water to a familia of Dz =15cm = 0.15 m. A3 = Ty (0.15)2 = Ty x0.225 = 0.01767 m2. Q1 = Q2 + Q3 Q = AIV, = 0.1767m3/3 02 = A2V2 = 0.0628 m3/J. 0, = 02+03 => 03 = 0.1139 m3/s Q3 = A3XV3 => V3 = 6.44 m/s .(AN). 0) The diumiders of a pipe at the sections @ and @ are 10cm and 15 cm respectively find the discharge through the pipe if the nelocity d,=10cm=0.10m d2 = 0.15 m.

#### BERNOULLI'S EQUATION

Euleria equation is derived by considering the granity and premure and the motion of fluid element is comidered along a stroam line.

It is known as equation equation of motion Bernoulli's equation is obtained by integrating the fuler's equation of motion.

gf flow is compressible s= c

$$\frac{p}{3} + gz + \frac{v^2}{2} = c$$

$$\Rightarrow \frac{p}{3g} + z + \frac{v^2}{2g} = c$$

Fg = presume energy per unit weight of fluid on presume head.

 $N_{2g}^{2} = \text{Kinetic energy per unit weight on Kinetic head.}$  z = potential head.

### Assumptions: \_

The following assumptions are taken on the dercivation of Bernoulli's equation.

- OThe fluid is ideal
- @ fluid in steady
- 3) The flow is trumpresible
- The flow in irrestational.

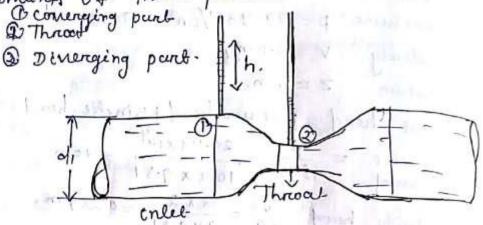
Wouter is flowing through a pipe of som diameter under a presume of 29.43 N/cm2 and with mean velocity of 2 m/s. Find the total head on total energy per unit weight of the water at a crom, - section which in 5m above the datum line. (Ans) Diameter of pipe = 5 cm = 0.5 m. pressure p = 29.43 N/cm2 = 29.43 x 10 N/m2. relocity V = 2.0 m/s Total head = presum head + winetic head + datum head present =  $\frac{p}{fg} = \frac{29.43 \times 10^4}{1000 \times 9.81} = 30 \text{ m}.$ velocity heavy =  $\frac{v^2}{29} = \frac{2 \times 2}{2 \times 9 \cdot 81} = 0.209 \, \text{m}$ . total head = fg + v2 +tz = 30 +0.204 +5 = 35.204 m. (Ans) a) A pipe through which water in flowing, in howing diameters 20 cm and 10 cm at the cream meetions of and 3 respectively. The velocity of water at section O is given 4.0m/s. Find the velocity head at rections and @ and also trate of discharge. D1 = 20 cm = 0.2m A1 = 0.0314 m2. V1 = 4.0 m/s . D2 = 0.1 m/s . Az = 0.00785m2. Qualouty head at rection ( = \frac{\sqrt{2}}{29} = 0.815 m. Q MED AIV, = A2V2 => V2 = 16 m/s relocity hered at rection @ = 83.047 m direhenry AIVI Ore AZV2 = F2. 0.125 6 m3/sec.

# Practical Applications of Berenoull's Theorem:

The rate of flow flowing through a pipe.

91 commints of three parts.

1 Throat part



-> consider a venturiemeter fitted in a horizontal pipe through which a fluid in flowing

of = cliameter at inlet ()

P1 = pressure at section ()

V1 = velocity of fluid at section ()

C1 = area at section ().

of 2 = diameter at section ()

P2 = pressure " "

V2 = velocity "

Applying Bernoulli's equation at  $\Phi$  and  $\Phi$   $\frac{P_1}{Jg} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{Jg} + \frac{V_2^2}{2g} + Z_2$   $\Rightarrow \text{pipe is horizontal}(Z_1 = Z_2)$   $\Rightarrow \frac{P_1}{Jg} + \frac{V_1^2}{2g} = \frac{P_2}{Jg} + \frac{V_2^2}{2g}$   $\Rightarrow \frac{P_1}{Jg} - \frac{P_2}{Jg} = \frac{V_2^2}{2g} - \frac{V_1^2}{2g}$   $\Rightarrow \frac{P_1 - P_2}{Jg} = \frac{V_2^2 - V_1^2}{2g}$ 

$$h = \frac{v_1^2}{2\eta} - \frac{v_1^2}{2g}$$

$$h = \frac{v_2^2}{2\eta} - \frac{v_1^2}{2g}$$

$$\Rightarrow h = \frac{v_2^2}{2\eta} - \frac{v_1^2}{2g}$$
Applying continuity equation
$$a_1v_1 = a_2v_2$$

$$\Rightarrow v_1 = \frac{a_2v_2}{a_1}$$

$$h = \frac{v_2^2}{2\eta} - \frac{\left(\frac{a_1v_2}{a_1}\right)^2}{2\eta}$$

$$= \frac{v_2^2}{2\eta} \left[1 - \frac{a_1^2}{a_1^2}\right]$$

$$= \frac{v_2^2}{2\eta} \left[1 - \frac{a_1^2}{a_1^2}\right]$$

$$= \frac{v_2^2}{2\eta} \left[\frac{a_1^2 - a_2^2}{a_1^2}\right]$$

$$v_2 = v_2^2 = 2\eta h \left(\frac{a_1^2 - a_2^2}{a_1^2 - a_2^2}\right)$$

$$\Rightarrow v_2 = 2\eta h \left(\frac{a_1^2 - a_2^2}{a_1^2 - a_2^2}\right)$$

$$\Rightarrow v_2 = 2\eta h \left(\frac{a_1^2 - a_2^2}{a_1^2 - a_2^2}\right)$$

$$\Rightarrow v_2 = \sqrt{2\eta} h \sqrt{a_1^2 - a_2^2}$$

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$$\Rightarrow v_1 = \sqrt{2\eta} h \sqrt{a_1^2 - a_2^2}$$

$$\Rightarrow v_2 = \sqrt{2\eta} h \sqrt{a_1^2 - a_2^2}$$

$$\Rightarrow coefficient of durbary. Or durbary.$$

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value of h' given by differential u-Tube amanometer  $h = \pi \left[ \frac{s_h}{s_n} - 1 \right]$ Sh = specific granity of a heavy liquid So = specific greenity of liquid flowing through por a clifference of the houser liquid column in ouit, u-tube. 91 [847 50] 91 SH ( 50  $h = \pi$  Se  $h = \pi \left(1 - \frac{Se}{So}\right)$ Se = sp. greatly of lighter liquid in U-tube (6) A horizontal venturimeter with inlet and throat dicemeters 30cm and 15cm respectficiely. The reading : differential manometers connected to the inclusions the throat is 20cm of Hg. Determine the nocte of the d1 = 30 cm 01 = 174912 = 706.85cm 2  $d_2 = 15 \text{ cm}$   $\alpha_2 = 176.7 \text{ cm}^2$ Cd =0.78. n = 20cm. h = n [ sh -1] = 20 [ 13.6 -1] =252.0 cm, of 420 Q = Cd \(\alpha\_1 \alpha\_2 \) \(\sigma\_1 \alpha\_2 \) \(\sigma\_2 \) \(\sigma\_1 \alpha\_2 \) \(\sigma\_2 \) = 125. 756 lt/ser. = 0.98 x

Applying Berenouli's equation at 
$$\mathbb{D}$$
 and  $\mathbb{D}$ 

$$\frac{P_1}{fg} + \frac{v_1^2}{2g} + Z_1 = \frac{P_2}{fg} + \frac{v_2^2}{2g} + Z_2$$

$$\frac{P_1}{fg} = \text{presume heard at } \mathbb{D} = 14$$

$$\frac{P_2}{fg} = \text{presume heard at } \mathbb{D} = (4+6)$$

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$$\frac{P_1}{fg} = \text{presume heard a$$

Of A pitot tube in invented in a pipe of 300mm diameter. The static premune in pipe in poomm of mercury (vaccum). The stagnation presume at the contre of the pipe,

The stagnation presume the recte of thow of water in 0.981 N/cm². Calculate the recte of thow of water through pipe, if the mean relocity of them in

O.85 times the certical valority take CV = 0.98.

 $A_{11}$   $d = 300 \, \text{mm} = 0.3 \, \text{m}.$   $a = \sqrt{4} \, d^2 = 0.07068 \, \text{m}^2$ 

static pressure head = 100 mm of Hy (vacuum).  $= \frac{-100}{1000} \times 13.6 = -1.36 \text{ m of consten}.$ 

$$\frac{-100}{1000} \times 9 \times 13.6 = (f)_{\omega} \times 9 \times h.$$

$$\Rightarrow h = \frac{-100}{1000} \times 9 \times 13.6 \times 13.6$$

stagnation prossure hered = 0.981×104 = 1 m.

velocity at centre = Cv X J2gh =0.98 X 2x9.81 x 2.36 = 6.668m/s. weboily = = = = x 0.85 x 6.668 = 5.66 78 m/s of thew = Vxarou = 0.4006 m3/s (Am)

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Edward W. Promotion

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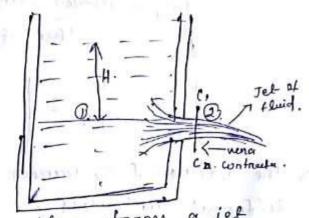
orcifice is a small opening of any cross section (such as circular, triangular, rectangular etc) on the ride on at the bottom of a fance, through which the fluid in flowing

ochsitication of orcidice !-

Flow through an orcifice ! -

-> consider a fluid fank filled with a circular orifice in one of its ricles.

-) Let H be the head of the liquid above the centre of the orietice.



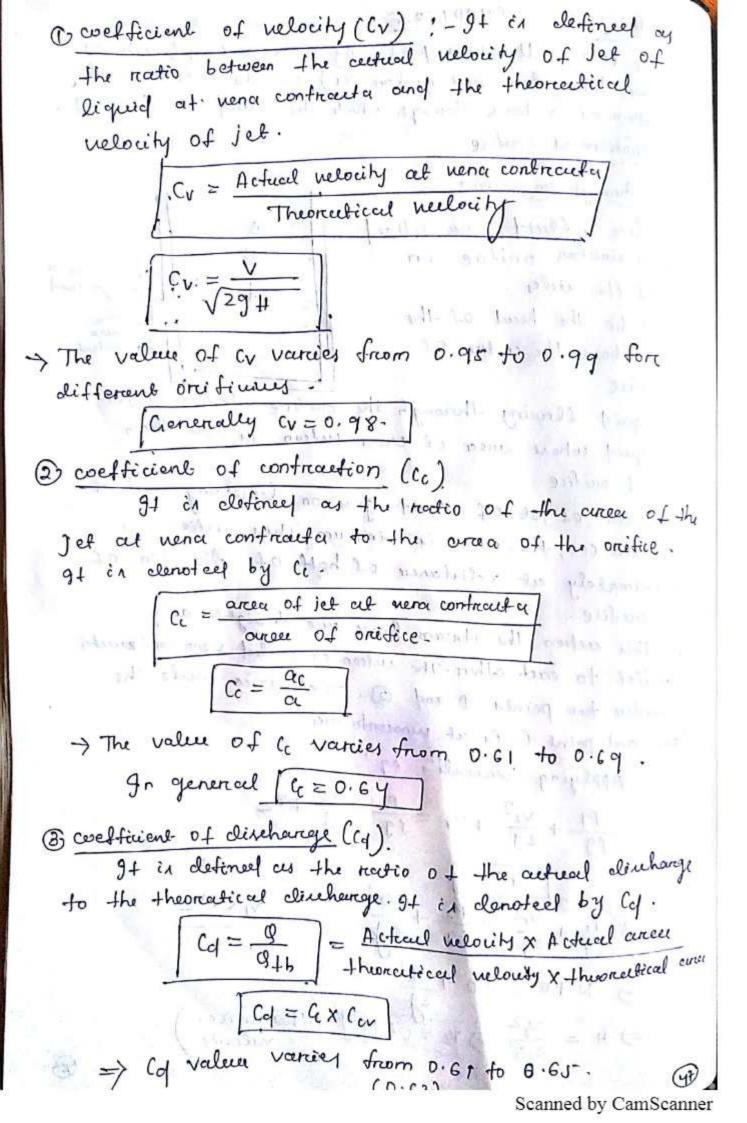
The liquid flowing through the orietice torins a jet Of liquid whose area of cross section is low than

The area of jet of fluid goes on decreasing and ala section C-C, the circa is minimum. This metion approximately est a distance of half of diameter of

> At this metion the stream lines are straight and parallel to each other. The rution is called vena conferenta. -> Consider two points @ and @. point D in inside the

tank and point & is at menaconfractor.

Applying Berrouli's eq?  $\frac{P1}{fg} + \frac{{v_1}^2}{2g} + Z_1 = \frac{P_2}{fg} + \frac{{v_2}^2}{2g} + Z_2$ => H+0= 0+ 122 =)  $H = \frac{\sqrt{2^2}}{29}$  =)  $\sqrt{2} = \sqrt{2917}$  (+heoretical



of the heered of water over an orcifice of diameter your is som find the actual discharge and the cutacel nularry of jet cet vence contracted. (d = 0.6 Cv = 0.98.

a), The heesel of water over the centre of an orifice of diameter 20 mm is 1m. The certical discharge through the orieties is 0.83. It /s. Find the Col.

$$\alpha = 0.8214/2 = 0.00082. m_3/2$$

$$cd = 0.61$$

Introduction; \_

A notch is a clevice used for measuring the rule of flow of a liquid through a small channel or a tank.

If may be defined as an opening in the ricle of a tank on a small channel in such a way that the liquid surfaces in the tank on channel is below the top edge of the opening.

open chained over which the flow occurs. It is generally in the form of vertical wall with a sharp edge cet the top.

The notch is of small size while the wein is of a bigger size.

The notch is generally made of metallic plate while the weir is made of concrete structure.

#### clamification

The notches are claufied as

CAccording to the shape of motels opening

(i) rectangular notch

(1i) trianguler notch

(iii) Traporoidal notch

(iv) stepped notch.

(i) Notch with and confraction

(ii) Notch without end contraction.

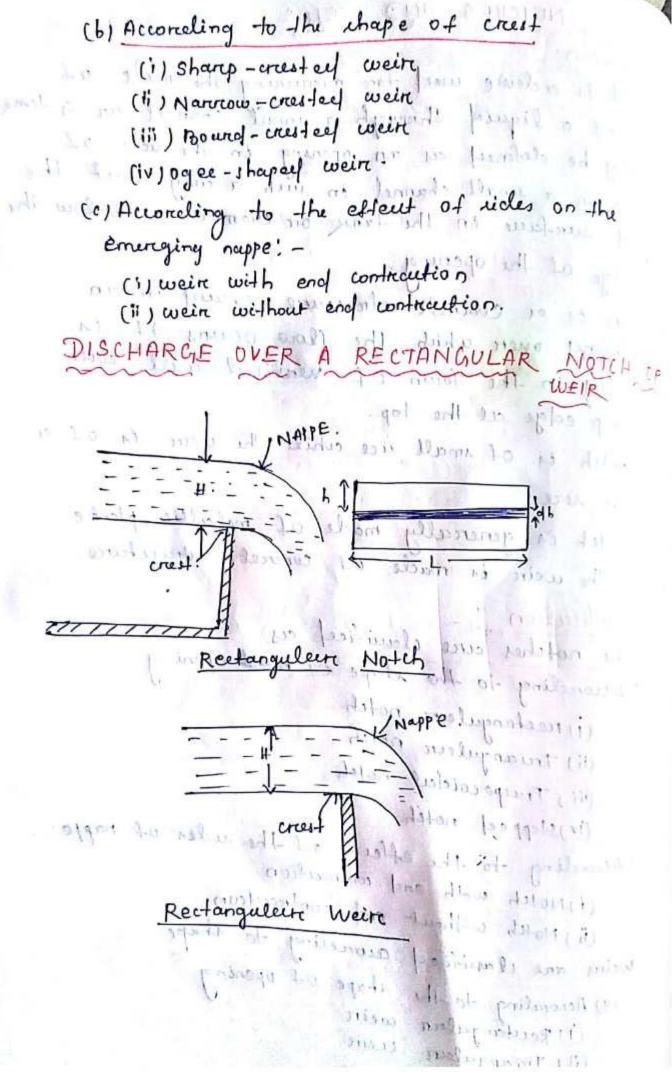
weires are classified awreling to shape

(9) According to the shape of opening

(1) Reutangulan wein

(ii) Triangular weire

(iii) Traperoidal weir.



comider a rectanguler notch or weir provided in a channel courseing water.

H = heard of water over the crest L = Length of the notch or weire.

To find the direhange of water flowing over the weire on notch, consider an elementary the weire on notch, consider on thickness of and horizontal straip of water of thickness of unface. length L at a depth h from the free unface.

Areer of strip = Lxdh.

theoretical velocity of water flowing through strip = 129h

The discharge do, through straip on

des = Cox area of strip x Theoretical nelocity

$$Cl = \int_{Col}^{H} Col \times L \times \sqrt{2gh} \times dh$$

$$= Col \times L \times \sqrt{2g} \times \int_{Col}^{H} h^{1/2} dh$$

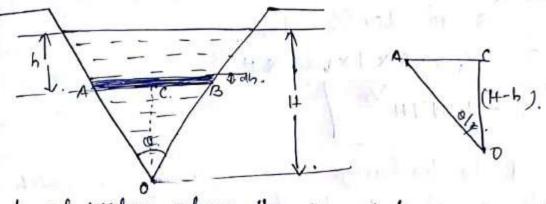
$$= col \times L \times \sqrt{2g} \times \int_{Col}^{H} h^{1/2} dh$$

$$= col \times L \times \sqrt{2g} \times \int_{Col}^{H} h^{1/2} dh$$

$$= col \times L \times \sqrt{2g} \times \int_{Col}^{H} h^{1/2} dh$$

$$= e^{\zeta_d \times L \times \sqrt{2g}} \times \frac{h^{3/2}}{3/2} \int_0^{4}$$

(2) Find the discharge of water flowing over rectangular notch of 2m length when the constant here over the notch in Boommi. Cof =0.60 Head over the notch! H = 300 mm = 0.30m Col = 0.601 ... L = 2 m Q = 2/3 Cd x L x \(\frac{29}{29}\) x (H 3/2)  $= \frac{2}{3} \times 0.6 \times 2.0 \times \sqrt{2} \times 9.81 \times (0.30)^{3}$ CS = 0.582m3/5 1 x1 - quito 1) Defermine the height of a rentangular ever leneith 6m to thebe built courses, a rectangular channel. The manimum length of water on the upstream side of the wir is 1.8 m and discharge C1 2000 litho /s. Take ( 'Cy = 0.60) L=6m. H1=1.8 m Q = 2000 lt/s.11 x d ( th) -1+2 Q = 2/3 Cd x L XV29 x H 3/2 => 2 = 3/3 × 0.6 × 6.0 × \2x 9.81 × H /2 => H3/2 = 2.0 = 0.858m = 1.8-0.328 = 1.472m.



H = head of water above the V-notch.

consider the horizontal strip of water of thickness 'dh' at a depth of h from the free uniform of

welfer.  $\tan \frac{0}{2} = \frac{AC}{OC} = \frac{AC}{(H-h)}$ 

Ac = (H-h) tan 0/2

AB = width of strip = 2x AC

= 2x (H-h) ten 0/2 x olb

Theoretical nelocity of water through stree p = 1296
Discharage through the streep

da = Cd x Area of strip x velocity = Cd x 2(H-h) ton % xdh x 29h

= 2x Gx (H-h) ten 1/2 x vegt x dh

a = 1 2 cd x (H-h) tan a/2 x v 2gh x dh

= 2 cd x tan 6/2 x 29 x (H-h) h /2 d h

= 2x Cd x tan 2 x \29 \ TH h 2 dh - 5h 3/2 dh

= 2x cd x tom 0/2 x \29 [ 2/3 H - 2/5 H 5/2

= 2 x C4 x tan 0/2 x \( \frac{4}{15} H^{5/2} \)

9 = 8/15 Cyx tan 0/2 XV 29 X H 5/2 for a v-notch Cy=0.C 0=90°, tan 0/2=1. 0= 8/15-X0.6X 1XV29 X H Q = 1.417H 5/2 1) Find the discharge over a triangular notch of angle Go" when the heard lover the V-notch in own Cd = 0.6 Am mi O = Go mistra to quity between it # = 0.3 m. 1511 11 munt of the digital Cd = 0.6 0 = 8/15- x Cd x tan 0/2 x 29 x H5/2 = 3/5 x 0.6 x tan 30 x (2x 9.81 x (0.3) 5/2 Q = 6.040 m3/s. (Ans) 110 x 10 mod (4 4) x refrent relocated at a completely the per guile 311. Aquandle of The wast of a party for a property of the second 96 - CAX 36 H P P FEB VX 48 A X 13 -Straff (4-4) x xxxxxxx 41 x 25 . . 1/2 mot (4-17) x 402 / At the file of the file of the file of 

## FLOW THROUGH PIPES (CHAPTER-6)

Lou of energy in pipe! -

when a fluid in flowing through a pipe, the fluid experiences some remistance du to which some of the energy of fluid in lost. This loss of energy in clauficel as follows.

#### Eenergy loss man 1 - 1 - 1

Major energy loss

There is due to freition. (al Darcey - Weis beech formules. (b) cherry's Formula.

the case of money (uit)

Minor energy loss

(a) Sudden enpancion of pipe (b) Sudden contraction of pepe

(c) Bend in pipe

(d) pipe tillings me, obstruction in pipe.

(1) Loss of energy due to friction.

(a) Duruy - Weisborch Formula: This loss of energy in pipes due to friction is calculated from Dancy - weisback equation. hf = 4+ Lv2

$$h_f = \frac{4 + L V^2}{299}$$

hy = Loss of head due to fraction. of = coefficient of friction = IG

$$f = \frac{16}{Re} \left( Re < 2000 \right)$$

$$f = \frac{0.079}{te^{1/4}} \left( Re \left( 4000 - 10^6 \right) \right)$$

$$L = Length of pipe.$$

V= mean velocity of flow

d = diameter of Pipe.

(b) chezy's formules The enpression for loss of here due to frieting hf = fl x PxLXV2 hf = loss of head due to friction A = area of cross - section of pipe p = welled perimeter of pipe v = mean nelocity of flow! p = percimeters of pipel. L = Length of pipe. A = Arcea of flow is called hydraulit meandy A = (hydraulic meen depth on hydraulic reading) (A/p) in denoted by m'. Luce of michigan .. hydraulic mean depth m= 4/p= Tryd = (4) A = m on (A) = /m. hy = + x L x V 2 x m.  $= \frac{1}{\sqrt{3}} \sqrt{3} = \frac{1}{\sqrt{3}} \sqrt{3} \times \sqrt{3} = \frac{1}{\sqrt{3}} \sqrt{3} \times \sqrt{3} = \frac{1}{\sqrt{3}} = \frac{1}{\sqrt{3}} \sqrt{3} = \frac{1}{\sqrt{3}} = \frac{1}{\sqrt{3}} \sqrt{3} = \frac{1}$  $\Rightarrow V = \sqrt{\frac{1}{100}} \times m \times \left(\frac{1}{100}\right)^{\frac{1}{1000}} = V = \sqrt{\frac{1}{1000}}$  $\Lambda = \sqrt{\frac{t_1}{3a}} \times \sqrt{\frac{r}{\mu t_1}}$ where I'm = c (c'=chery's constant) This Is known as chezy's foremules.

Q), Find the head lost due to fruition in a pipe of diameter 300mm and longth som through which water is flowing at a relouty of 3m/s . ming (i Dany , formules Data Y = 0.01 Home) (ii) Chery's formules. d = 300mm = 0.30m. 1 = 0.01 14010 = 0.01 x 10 4 m2/ L = 50 m. v = am/s. C = 60 . Yours one  $Re = \frac{Vol}{v} = \frac{3 \times 0.30}{0.01 \times 10^{-4}} = 9 \times 10^{5}$ (i) hf = 4xfx Lxv2 · (charges formula)  $= \frac{4 \times 6}{4 \times 0.0025 \times 50 \times 3^{2}}$   $= \frac{4 \times 6}{0.3 \times 2 \times 9.81}$ he = 0.7828 m (ans) (ii) chezy's formules. v z cvmi c=60., m= d/y = 0.3 = 01075m. V=c XVmi => 3 = 60 x 0.075 x hf => (= 3) = 0.075 × hit > ht = (3) X - 0.075 ht = (3) 2 x 0.075 x 50 = 1.665 m. (And)

Minor Energy Losses:

The loss of energy due to freition in pipe is known as major loss while the loss of energy due to change of relocity of the for their is called minore loss of energy.

consider a liquid flowing through a pipe which has sudden enlargement as shown on rabone tique. consider two rections O-O and 3-D before and after enlargement.

P<sub>1</sub> = pressure intensity at section 0 - 0 V<sub>1</sub> = velocity of flow at section 0-0 Cu<sub>1</sub> = area of pipe at section 0-0. P<sub>2</sub> = pressure intensity ut section 2-2. V<sub>2</sub> = velocity of flow at section 2-2 Cu<sub>2</sub> = area of pipe at section 2-2.

Due to sudden change in diameter of pipe from DI to Dz, the liquid flowing from the smaller pipe is not able to follow the change of boundary Thus the flow separates from the boundary and turbulent eddies are formued.

The loss of energy tomes planes oleve to force, of these eddies. 917 p'= pressure intensity of the liquid eddles he = LOM OI head du to suelden enlargement Applying Bernoulli's equation P1 + V12 + Z1 = P2 + V2 + Z2 + head lose  $\Rightarrow$   $|z_1 = z_2|$  $\frac{p_1}{39} + \frac{v_1^2}{29} = \frac{p_2}{39} + \frac{v_2^2}{29} + he$ => he = \( \frac{P1}{P9} - \frac{P2}{19} \) + \( \frac{V1}{29} - \frac{V2}{29} \) -> The force acting on the liquid in the central volume in the direction of flow is given by Fx = P. A++P (A2-A1)-P2A2 1 - 1000 rections to local &- 6,9=19 . . . Fx = P1 A1 +P1 (A2 -A1) -P2A2 = P1A2 - P2A2 Fx = A2 (P1-P2). in 12 100 in 12 10 = 1 Momentum of liquid in section 1-1 = 8, A, V,2 momentum of liquid at section 2-2 = 8 A21/2 change in momentum = 8A2V2 - 8 A1V12 continuity equelion [AIVI = AZVZ]  $A_1 = \frac{A_2 \vee 2}{\vee 1} \quad \text{and } \quad A_2 \vee 2$ change in momentum/sec = 8 A2V22 - 8 x A1V12  $= \$A_2 \vee_2 ^2 - \$ \times \underbrace{A_2 \vee_2}_{V_1} \times \vee_2 ^2$ = 8 A2V2 = 8 A2V1V2 10 wilder washing = 8 A 2 ( V2 - V1 V2)

Net force certing on control volume in the direction of flow must be equal to the rate of change of ntum. ( $P_1-P_2$ )  $A_2 = SA_2 (V_2^2 - V_1 V_2)$ momentum  $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$   $= \sum_{n=1}^{\infty} \frac{p_2 - p_2}{dt} = V_2^2 - V_1 V_{12}$ infamiliar care to familia in ing of the board to specifical : he =  $\left(\frac{P_1}{89} - \frac{P_2}{89}\right) + \left(\frac{v_1^2}{29} - \frac{v_2^2}{29}\right)$  $= \frac{v_2^2 - v_1 v_2}{9} = + \frac{v_3^2}{29} = \frac{v_2^2}{29} = \frac{v_2^2}{29} = \frac{v_3^2}{29} = \frac{v_3^$ 242 - 24142 + 42 - 42 is a probable of the phenology is V22+V12 = 2V1 V2 | 100 10 100 100 he = No - Va)2 he =  $\frac{(v_1 - v_2)^2}{29}$ Low of Head den to Sudden Contraction

> Comider a liquid flowing in a pipe which has sudden contraction in around as ahown in fig. I woulder two section (1-1) and (2-2) before and after contraction.

→ An the liquid goes from a larige pipe to a small pipe, the area of flow goes on decreasing and becomes minimum at section (C-1). This rection of it called as were confracted.

After rection (-1, a medden enlargement tames plans)

The low of head due to medden contraution in

actually due to medden enlargement from

mera contracte to maller pipe.

Let Ac = Area of flow at section C-i.

Vc = velocity of flow at section C-C.

Az = Area of flow at section 2-2.

Vz = velocity of flow at section 2-2.

hc = LOAA of head dece to sudden contraction.

$$h_{c} = \frac{(v_{c} - v_{2})^{2}}{2g}$$

$$= \frac{v_{2}^{2}}{2g} \left[ \frac{v_{c}}{v_{2}} - 1 \right]^{2}$$

freom continuity equation  $AcVc = A_2V_2$   $\frac{Vc}{V_2} = \frac{A_2}{AC}$   $\Rightarrow \frac{Vc}{V_2} = \frac{1}{C_c}$   $\Rightarrow \frac{Vc}{V_2} = \frac{1}{C_c}$   $\Rightarrow \frac{Vc}{V_2} = \frac{1}{C_c}$ 

where 
$$K = \left(\frac{1}{C_c} - 1\right)^2$$
 $h_c = \frac{K v_c^2}{2g}$ 
 $C_c = 0.62$ 
 $h_c = 0.375 \frac{v_c^2}{2g}$ 

The conduction of piven then

 $h_c = 0.5 \frac{v_c^2}{2g}$ 

The law of head when the pipe of diameter stooms in modernly enforcing to a diameter of yours . The racte of flow of waller through the pipe in 2sylino/sec.

The sylves  $m_c = 0.2m$ 
 $m_c = 200 \text{ mm} = 0.2m$ 
 $m_c = 11/4 p_c^2 = 11/4 \times (0.2)^2 = 0.03 \text{ M/s} \text{ m}^2$ 
 $m_c = 11/4 p_c^2 = 11/4 \times (0.4)^2 = 0.12564 \text{ m}^2$ 
 $m_c = 250 \text{ line}/J_c = 0.25 \text{ m}^2/J_c$ 
 $m_c = 250 \text{ line}/J_c = 0.25 \text{ m}^2/J_c$ 
 $m_c = 240 \text{ line}/J_c = 0.25 \text{ m}^2/J_c$ 
 $m_c = (v_1 - v_2)^2 = (3.96 - 1.99)^2$ 
 $m_c = (v_1 - v_2)^2 = (3.96 - 1.99)^2$ 
 $m_c = (4.96 - 1.99)^2$ 

1 9 pt sains N

the Kit well-broad to the filter that

3) LOSA of Head at the Entrance of Pipe. This is the loss of energy which occurs when a liquid entere a pipe cohich is connected to large tank.  $hi = 0.5 \frac{\sqrt{2}}{29}$ v = relowing of liquid in pipe. 4) Low of Head at the Enit of pipe ! -This is loss of head due to relocity of liquid at the outlet of pipe: 9+ in elenoteelas ho  $h_0 = \frac{v^2}{2g}$  v = velocity of liquid of outlet of pipe.5) Louis of head due to Bend in pipe ! when there is bend in pipe , the nelocity of flow changes due to which formation of eddies  $h_b = \frac{Kv^2}{2g}$ takes place.

hb = whom of head due to bend. ~ = velocity of flow. K = wef-ficient of bend.

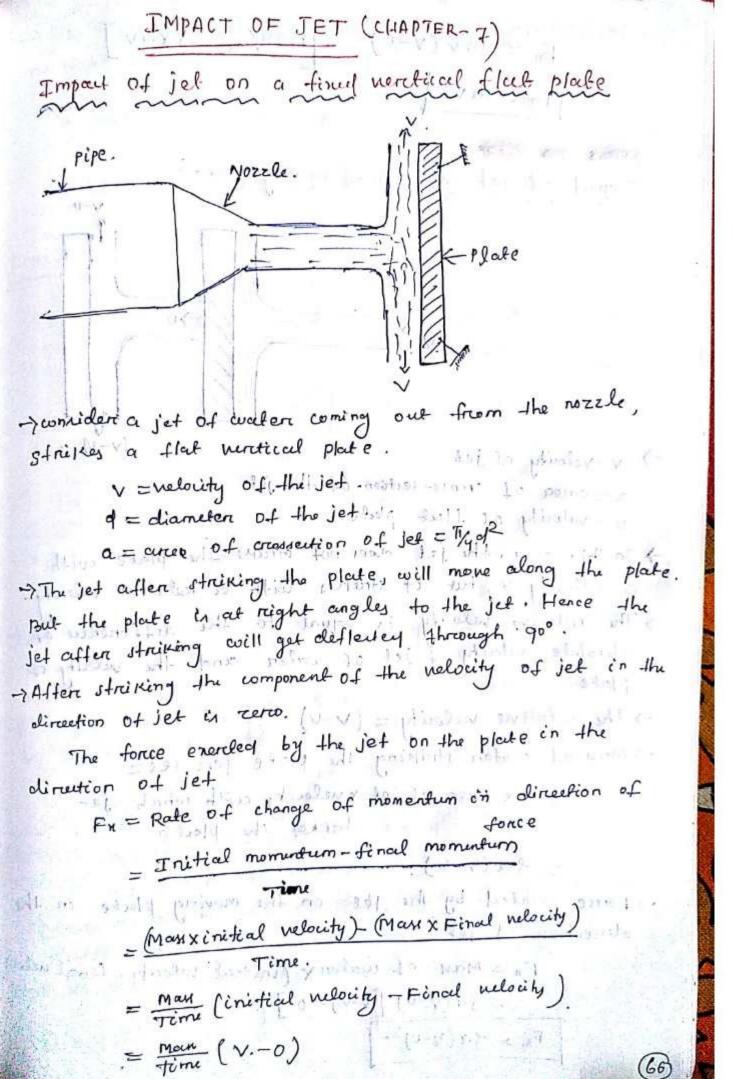
6) Long of Head in various pipe fettings This is the low of head in various pipe fittinge. 9+ is expressed cy

V= whomby of flow. KE coefficient of Pipe Lile.

#### HYDRAULIC GRADIENT LINE

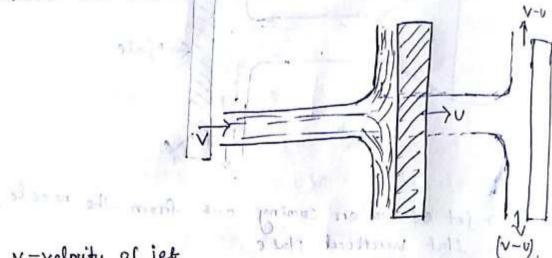
9+ is defined as the line which gives the un of pressure head ( ! ) and datum head ( z ) of a flowing fluid in a pipe with respect to some reference line. 79+ in briefly written as H.G.L (Hydraulic gradient) TOTAL ENERGY LINE ! -

9t is defined as the line which gives the rum of pressure head, datum head and rinetic head of a flowing fluid in a pipe with respect to some -> 9+ à bruefly written ou TE.L (Total Energy Line). reference line.



FORBAN TOO PERENT

Impact of jet on ventical moving plate:



> v=velocity of jet a = circa of cross-section of the jet v = velocity of flut plate. Il la notamon.

> In this care, the jet does not strike the plate with a nelocity v, but it struckes with a relative velocity. > The relations velocity in equal to the difference of absolute nelowity of jet of water and the velocity of

-> The relative velocity = (v-v)

-> Man of water striking the plate per see = fx Area of jet x velocity couth which jet string the place. muleuman garten

= 8-ex (v-v)

-> Force enerted by the jet on the moving place in the direction of jet

Fn = Man of water x (initial velocity - final webs) = 8a(v-v) [(v-v) - 0]

Fx = 1a(V-U)2

> The worck will be done by the jet on the place, ou place is moving. workdone = Force x relocity = Fx X U = fa(v-v)2xv enerted by a jet of waler, on a series of varies corce e jet of wider. >90 actual practice, a large number of plates are mounter on the circumferoneu of a wheel at a fined distance > The jet strives a plate and due to the force enember by the jet on the place, the wheel stands moving. N=nelocity of jet. d = diameter of jet. a = cron - netional area of jet = 1/4 d2 u = velocity of varie. -> man of water per second straining the series of -) jet straines the place with a relocity = (v-v)

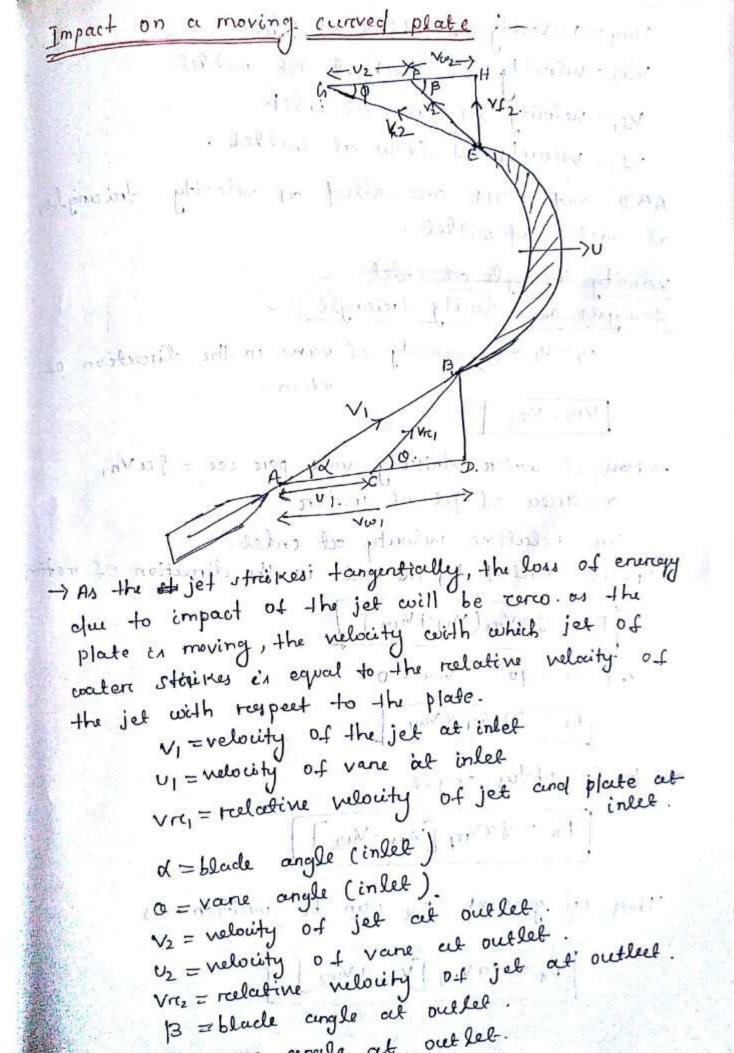
-> The force enembed by the jet in the direction of motion of place Fn = man at x (initial relocity - final relocky = 3 av[(v-v)-0] Fi = fav(v-v) workdone = Force & Distance relocity = Fx X U W = fav (v-v) x v Kirutic energy of the jet per second = 1/2 my 2 = bjav x v2 KE = 1/2 9 av 3 1= workdone per record K.E per second ? fav (v-v) x v = 2v (v-v) condition for Maximum Efficiency dn = 0  $\Rightarrow \frac{d}{dv} \left( \frac{2v(v-v)}{v^2} \right) = 0.$  $\Rightarrow \frac{d}{dv} \left( \frac{2vv - 2v^2}{v^2} \right) = 0$  $\Rightarrow \frac{2v - 2x 2u}{v^2} = 0$ =) 24-40=0  $\Rightarrow$   $v = \pm v = \sqrt{v} = \sqrt{2}$ 

Manimum efficieny
$$\eta_{max} = \frac{2v(v-v)}{v^2}$$

$$= \frac{2v(2v-v)}{(2v)^2}$$

$$= \frac{2v \times v}{4v^2} = \frac{1}{2} = 50', \quad \square$$

$$\eta_{max} = 50'.$$



φ = vaine cengle at outlet.

Vw1 = relocity of whire cet inlet Vw2 = relocity of exceptive act outlet Vs, = nelocity of slow at inlet VI2 = velocity of flow at outlet. ABD and EAH are called as relocity triangle at inlet and outlet. velocity triangle cot inlet: -Analysis of nelocity traingle U1 = U2 = U = valocity of vane in the direction of motion. V11 = V12 -> man of water striking vare per see = fav, a = area of jet of water. Vr. = relative velocity at inlet. -> porce enerched by the jet in the direction of moti Fx = favry (Vw1+Vw2) 9 f 13 = 900, Vwz = 0! 100/20 1; 12/11/2  $F_{X} = f_{a} V_{R_{1}} \times v_{w_{1}}$   $F_{X} = f_{a} V_{R_{1}} \times v_{w_{1}}$   $F_{X} = f_{x} V_{R_{1}} \times v_{w_{1}}$ > 13, is obtus angle Fr = favre, [Vw1-Vw2] Thus in general Fre can be written as  $F_{n} = g_{\alpha} V_{\kappa_{1}} \left[ V_{\omega_{1}} \pm V_{\omega_{2}} \right]$ The alpha Double of Bay the Br Mar

-> workdone per sewnd on the vane by jel-= Fx X U W = favn, [Vw, ± Vw,] x U efficiency of jet: n = butput = coordictions per second on the varie K.E fark, (Vw1 ± Vw2 ) XU 1 m V12 gavni (Vwi + Vw2) x U 1 x Ja Vn, X V, 2  $= \frac{(\vee \omega_1 \pm \vee \omega_2) \times U}{\pm \times \vee^2}$